

6.1 a) 1. Collapse nodes with transmittancies ± 1 .

2. Introduce node numbers according to the figure below.

3. Remove all delay elements

4. Initial nodes : v_1, v_2, v_3, v_4, x
 Executable operations: b_1, b_2, b_3, b_4

New nodes: u_1, u_2, u_5, u_6

Executable operations: $+, +$

New nodes: u_3, u_7

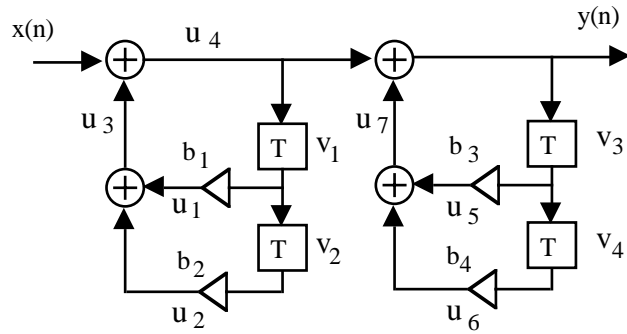
Executable operations: $+$

New nodes: u_4

Executable operations: $+$

New nodes: y

5. Complete the computation graph by adding the branches from the signal-flow graph. Note that the delay element $v_3(n)$ does not correspond to physical memory.



b) The system of difference equations is

$$\begin{aligned} u_1 &:= b_1 v_1(n) \\ u_2 &:= b_2 v_2(n) \\ u_5 &:= b_3 v_3(n) \\ u_6 &:= b_4 v_4(n) \\ u_3 &:= u_1 + u_2 \\ u_7 &:= u_5 + u_6 \\ u_4 &:= u_3 + x(n) \\ y(n) &:= u_4 + u_7 \\ v_2(n+1) &:= v_1(n) \\ v_4(n+1) &:= v_3(n) \\ v_1(n+1) &:= u_4 \\ v_3(n+1) &:= y(n) \end{aligned}$$

An intermediate node (u_i) can be eliminated if it appears only in one place on the right hand side. Thus, we can, for example, eliminate u_1 . We get

$$\begin{aligned} u_4 &:= b_1 v_1(n) + b_2 v_2(n) + x(n) \\ y(n) &:= u_4 + b_3 v_3(n) + b_4 v_4(n) \\ v_2(n+1) &:= v_1(n) \\ v_4(n+1) &:= v_3(n) \\ v_1(n+1) &:= u_4 \\ v_3(n+1) &:= y(n) \end{aligned}$$

c)

