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Note to Instructors

The solutions manual for the book can be found on the author's webpage at http://www.es.isy.liu.se/publications/books/Analog_Filters_Using_MATLAB/. Supplementary information can also be found on the author's webpage.