



Linköping University

xsens



UPPSALA
UNIVERSITET

An optimization-based approach to human body motion capture using inertial sensors

*TAR 2015: Technically Assisted Rehabilitation,
Berlin, Germany, 12-13 March 2015*

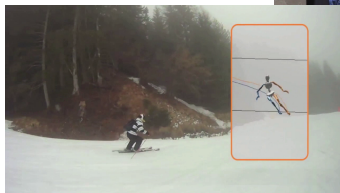
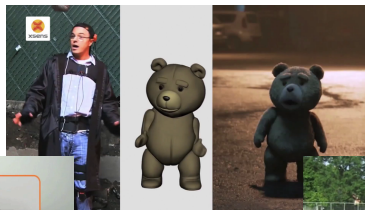
Manon Kok¹, Jeroen D. Hol² and Thomas B. Schön³

¹Linköping University, Sweden

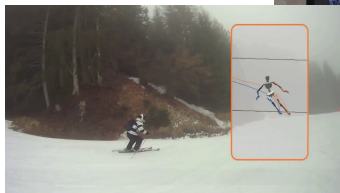
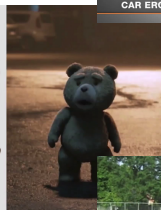
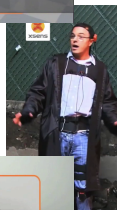
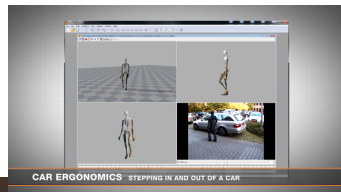
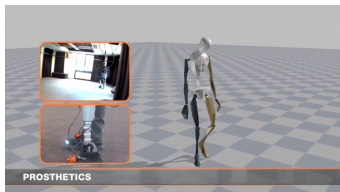
²Xsens Technologies, the Netherlands

³Uppsala University, Sweden

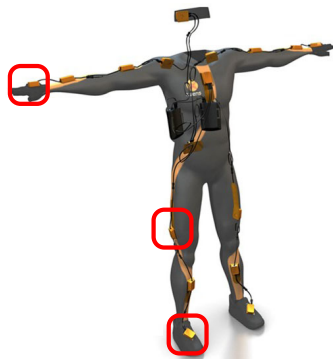




Applications of inertial motion capture

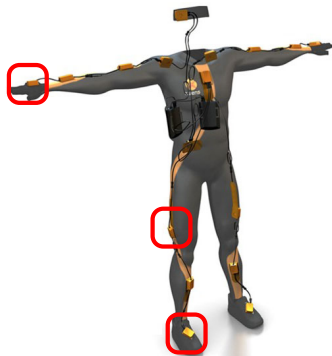
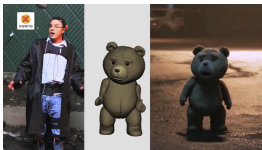






17 sensors placed on the body

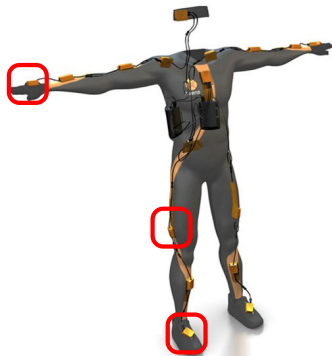
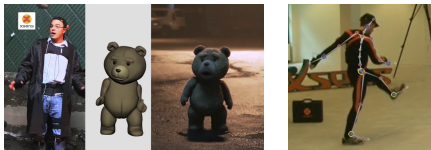
Estimate the relative position and orientation of body segments.



17 sensors placed on the body

Estimate the relative position and orientation of body segments.

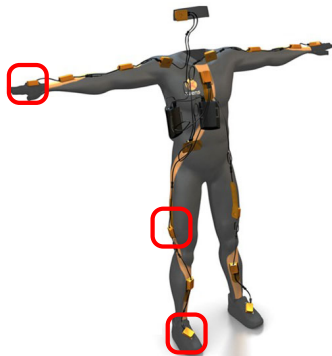
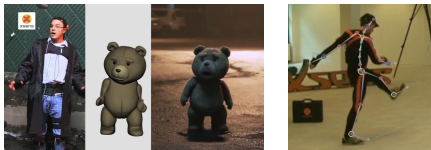
Possibly also estimate the body's absolute position.



17 sensors placed on the body

Estimate the relative position and orientation of body segments.

Possibly also estimate the body's absolute position.



17 sensors placed on the body

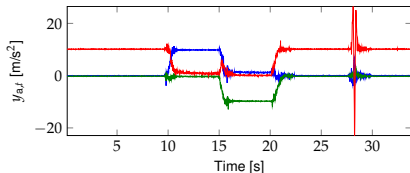
- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors



- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors

Accelerometer measures:

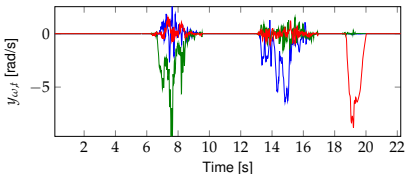
- Sensor's acceleration
⇒ Change in position
- Direction of gravity
⇒ Inclination



- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors

Gyroscope measures:

- Sensor's angular velocity
⇒ Change in orientation



- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors

Magnetometer measures:

- The local magnetic field
⇒ Heading (provided that magnetic field is not disturbed)

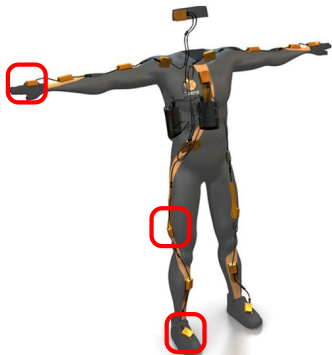


- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors



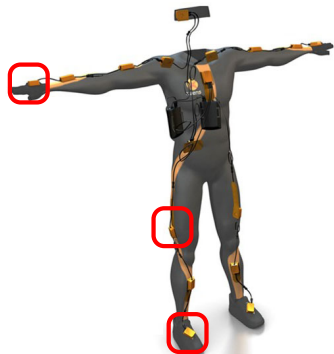
Inertial sensors and magnetometers are often used for orientation estimation. They also provide information about the change in position.





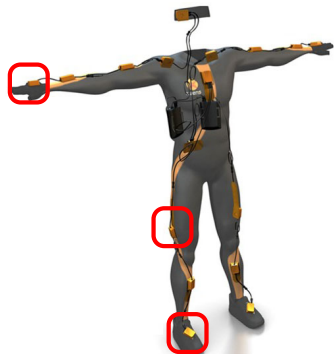
- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors

The magnetic field at the different sensor locations is typically different.



- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors

The magnetic field at the different sensor locations is typically different.



- Accelerometers
 - Gyroscopes
 - Magnetometers
- } Inertial sensors
- + Biomechanical model

Assuming that the body segments are connected to each other, the *relative* position and orientation of the body is observable (if the subject is not standing completely still).

We solve the motion capture problem by solving a *maximum a posteriori* (MAP) problem

$$\begin{aligned} \min_{z=\{x_{1:N}, \theta\}} & \underbrace{-\log p(x_1 | y_1) - \log p(\theta)}_{\text{initial state + prior}} \\ & \underbrace{-\sum_{t=2}^N \log p(x_t | x_{t-1}, \theta)}_{\text{dynamic model}} - \underbrace{\sum_{t=1}^N \log p(y_t | x_t, \theta)}_{\text{biomechanical/sensor model}} \\ \text{s.t.} & \underbrace{c_{\text{bio}}(z) = 0}_{\text{biomechanical model}} \end{aligned}$$

We solve the motion capture problem by solving a *maximum a posteriori* (MAP) problem

$$\begin{aligned} \min_{z=\{x_{1:N}, \theta\}} & \underbrace{-\log p(x_1 | y_1) - \log p(\theta)}_{\text{initial state + prior}} \\ & \underbrace{-\sum_{t=2}^N \log p(x_t | x_{t-1}, \theta)}_{\text{dynamic model}} - \underbrace{\sum_{t=1}^N \log p(y_t | x_t, \theta)}_{\text{biomechanical/sensor model}} \\ \text{s.t.} & \underbrace{c_{\text{bio}}(z) = 0}_{\text{biomechanical model}} \end{aligned}$$

$x_{1:N}$: time-varying states such as the sensor positions, velocities and orientations, the body segment positions and orientations.

θ : constant model parameters such as sensor biases.

$y_{1:N}$: inertial measurements.

We solve the motion capture problem by solving a *maximum a posteriori* (MAP) problem

$$\begin{aligned} \min_{z=\{x_{1:N}, \theta\}} & \underbrace{-\log p(x_1 | y_1) - \log p(\theta)}_{\text{initial state + prior}} \\ & \underbrace{-\sum_{t=2}^N \log p(x_t | x_{t-1}, \theta)}_{\text{dynamic model}} - \underbrace{\sum_{t=1}^N \log p(y_t | x_t, \theta)}_{\text{biomechanical/sensor model}} \\ \text{s.t.} & \underbrace{c_{\text{bio}}(z) = 0}_{\text{biomechanical model}} \end{aligned}$$

$c_{\text{bio}}(z)$: constraints imposed by the biomechanical model.

We solve the motion capture problem by solving a *maximum a posteriori* (MAP) problem

$$\begin{aligned} \min_{z=\{x_{1:N}, \theta\}} & \underbrace{-\log p(x_1 | y_1) - \log p(\theta)}_{\text{initial state + prior}} \\ & \underbrace{-\sum_{t=2}^N \log p(x_t | x_{t-1}, \theta)}_{\text{dynamic model}} - \underbrace{\sum_{t=1}^N \log p(y_t | x_t, \theta)}_{\text{biomechanical/sensor model}} \\ \text{s.t.} & \underbrace{c_{\text{bio}}(z) = 0}_{\text{biomechanical model}} \end{aligned}$$

$c_{\text{bio}}(z)$: constraints imposed by the biomechanical model.

\Rightarrow A constrained nonlinear weighted least-squares problem.

We solve the motion capture problem by solving a *maximum a posteriori* (MAP) problem

$$\begin{aligned} \min_{z=\{x_{1:N}, \theta\}} & \underbrace{-\log p(x_1 | y_1) - \log p(\theta)}_{\text{initial state + prior}} \\ & \underbrace{-\sum_{t=2}^N \log p(x_t | x_{t-1}, \theta)}_{\text{dynamic model}} - \underbrace{\sum_{t=1}^N \log p(y_t | x_t, \theta)}_{\text{biomechanical/sensor model}} \\ \text{s.t.} & \underbrace{c_{\text{bio}}(z) = 0}_{\text{biomechanical model}} \end{aligned}$$

$c_{\text{bio}}(z)$: constraints imposed by the biomechanical model.

⇒ A constrained nonlinear weighted least-squares problem.

Solve this as a batch problem using standard solvers.



The body segments are connected at the joints.



The body segments are connected at the joints.

⇒ **constraint**



The body segments are connected at the joints.

⇒ **constraint**

The position and orientation of the sensors on the body is approximately constant.



The body segments are connected at the joints.

⇒ **constraint**

The position and orientation of the sensors on the body is approximately constant.

⇒ **objective function**



The body segments are connected at the joints.

⇒ **constraint**

The position and orientation of the sensors on the body is approximately constant.

⇒ **objective function**

Some joints are restricted in their rotational freedom (optional).



The body segments are connected at the joints.

⇒ **constraint**

The position and orientation of the sensors on the body is approximately constant.

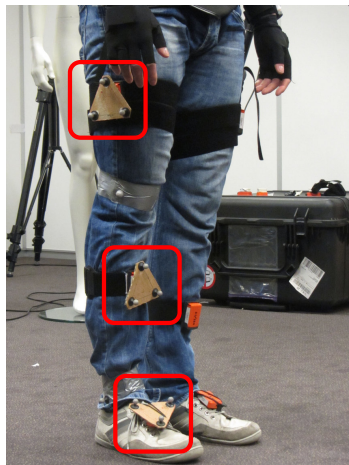
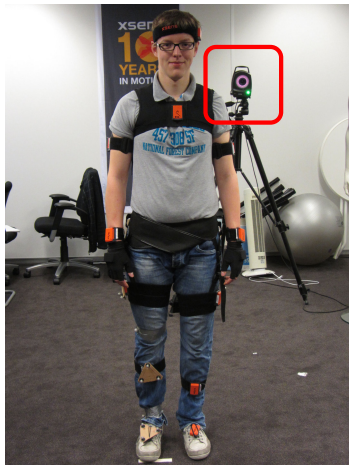
⇒ **objective function**

Some joints are restricted in their rotational freedom (optional).

⇒ **objective function**

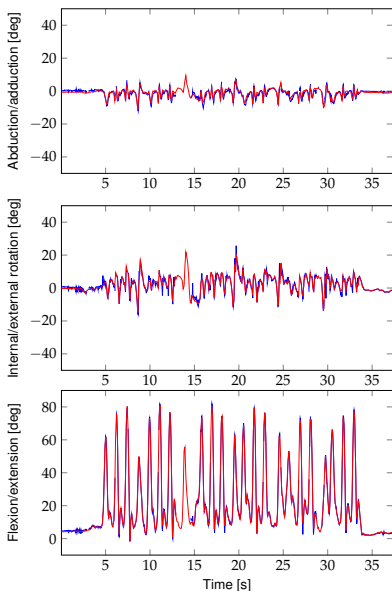
Experimental setup





Markers for an optical reference system

Knee joint angle estimates



Angle between the sensors on the upper and lower leg while walking.

Blue: Optical reference
Red: Estimates from our algorithm

Results using our algorithm.



Show movie

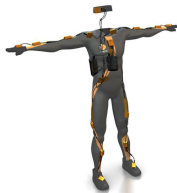
- We estimate the body's relative position and orientation using inertial sensors placed on multiple body segments.
- We obtain the estimates by solving a constrained optimization problem, where we make use of a biomechanical model.
- Our algorithm is shown to result in accurate joint angle estimates as compared to an optical reference system.



More information:

- The extended abstract for the conference.
- Manon Kok, Jeroen Hol and Thomas Schön, **An optimization-based approach to human body motion capture using inertial sensors.** *Proceedings of the 19th World Congress of the International Federation of Automatic Control*, 2014.

<http://users.isy.liu.se/en/rt/manko/>



Thank you for your attention!

Questions?

This work is supported by
MC Impulse, a European Commission,
FP7 research project,
CADICS, a Linnaeus Center
funded by the Swedish Research Council (VR)
and
BALANCE, a European Commission,
FP7 research project.

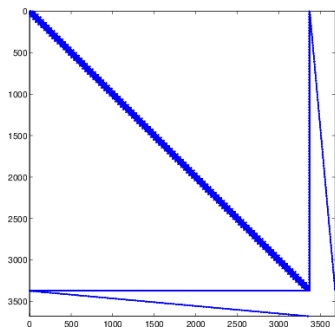


Thank you for your attention!

Questions?

This work is supported by
MC Impulse, a European Commission,
FP7 research project,
CADICS, a Linnaeus Center
funded by the Swedish Research Council (VR)
and
BALANCE, a European Commission,
FP7 research project.

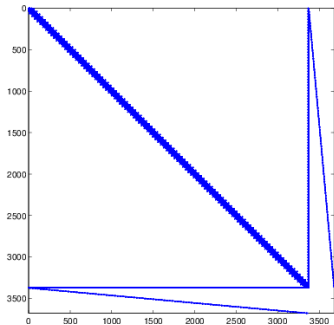




Only 0.56% of the matrix-elements are non-zero.

Solving the problem for an experiment of 10 seconds takes:

- about 5 minutes on an AMD X4 2.8 GHz processor (first inefficient Matlab implementation).
- Initial tests with a C-implementation show that speed improvements of up to 500 times are easily obtained.
- A moving horizon implementation would further speed up the computations.



Only 0.56% of the matrix-elements
are non-zero.

$$z \in \mathbb{R}^{(9N_S + 6N_B + 3)N + 3N_S}$$

equality constraints: $3N$

Example:
7 body segments, 7 sensors,
10s, 10Hz

⇒

~ 11000 variables
300 constraints

