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#### Contribution

A sensor fusion method for state estimation of a flexible industrial robot is presented. By measuring the acceleration at the end-effector, the accuracy of the arm angular position is improved significantly. The technique is verified on experiments on the ABB IRB4600 robot.

#### Introduction

Industrial robot control is based only on measurements from the motor angles. The aim here is to evaluate the

- extended Kalman filter (EKF)
- particle filter (PF)

for estimation of the end-effector position with



- motor angles, and
- end-effector acceleration,

as measurements using a state space model with *linear dynamic*.

#### **Bayesian Estimation**

Consider the discrete state-space model

$$\mathbf{x}_{t+1} = f(\mathbf{x}_t, \mathbf{u}_t, \mathbf{w}_t),$$
$$\mathbf{y}_t = h(\mathbf{x}_t) + \mathbf{e}_t,$$

with state variables  $\mathbf{x}_t \in \mathbb{R}^n$ , input signal  $\mathbf{u}_t$  and measurements  $\mathbb{Y}_t =$  $\{\mathbf{y}_i\}_{i=1}^t$ , with known probability density functions (PDFs) for the process noise,  $p_w(\mathbf{w})$ , and measurement noise  $p_e(\mathbf{e})$ .

The EKF linearises the nonlinear model around the previous estimate giving a time variant linear system where the Kalman filter can be applied.

The PF approximates the density  $p(x_t | \mathbb{Y}_t)$  by a large set of N particles  $\{x_t^{(i)}\}_{i=1}^N$ , where each particle has an assigned relative weight  $\gamma_t^{(i)}$ , chosen such that all weights sum to unity. The particles and weights are updated with each new observation.

### Models

A linear state space model for the dynamics with arm angles, arm velocities and arm accelerations as state variables, together with bias terms compensating for model errors and sensor drift, is proposed.

## **Estimation for Control of a** Flexible Industrial Robot

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The state vector is given by

$$\mathbf{x}_t = \left(\mathbf{q}_{a,t}^T \ \dot{\mathbf{q}}_{a,t}^T \ \ddot{\mathbf{q}}_{a,t}^T \ \mathbf{b}_{m,t}^T \right)$$

where  $\mathbf{q}_{a,t}$  contains the arm angles from joint 2 and 3,  $\dot{\mathbf{q}}_{a,t}$  is the angular velocity,  $\ddot{\mathbf{q}}_{a,t}$  is the angular acceleration,  $\mathbf{b}_{m,t}$  is the bias terms for the motor angles, and  $\mathbf{b}_{\dot{\rho},t}$  is the bias terms for the acceleration at time t. This yields the following state space model in discrete time

> $\mathbf{x}_{t+1} = \mathbf{F}_t \mathbf{x}_t + \mathbf{G}_{u,t} \mathbf{u}_t + \mathbf{G}_{u,t} \mathbf{u}$  $\mathbf{y}_t = h(\mathbf{x}_t) + \mathbf{e}_t,$

where

$$\mathbf{F}_{t} = \begin{pmatrix} \mathbf{I} \ T\mathbf{I} \ T^{2}/2\mathbf{I} \ \mathbf{0} \ \mathbf{0} \\ \mathbf{0} \ \mathbf{I} \ T\mathbf{I} \ \mathbf{0} \ \mathbf{0} \\ \mathbf{0} \ \mathbf{0} \ \mathbf{I} \ \mathbf{0} \\ \mathbf{0} \ \mathbf{0} \ \mathbf{I} \ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \\ \mathbf{0} \ \mathbf{0} \\ \mathbf{0} \ \mathbf{0} \\ \mathbf{0} \ \mathbf{0} \\ \mathbf{0} \\$$

The input,  $\mathbf{u}_t$ , is the arm jerk reference, i.e., the differentiated arm angular acceleration reference.

The observation relation is given by

 $h(\mathbf{x}_t) = \begin{pmatrix} \mathbf{q}_{m,t} + \mathbf{b}_{m,t} \\ \ddot{\boldsymbol{\rho}}_t + \mathbf{b}_{\ddot{o},t} \end{pmatrix}$ 

where

$$\mathbf{q}_{m,t} = r_g^{-1} \Big( \mathbf{q}_{a,t} + k^{-1} \Big( M_a(\mathbf{q}_{a,t}) \ddot{\mathbf{q}}_{a,t} + g(\mathbf{q}_{a,t}) + C(\mathbf{q}_{a,t}, \dot{\mathbf{q}}_{a,t}) \dot{\mathbf{q}}_{a,t} \Big) \Big)$$

is the motor angles from the robot dynamic equation and

$$\ddot{\boldsymbol{\rho}}_{b,t} = \mathbf{J}(\mathbf{q}_{a,t})\ddot{\mathbf{q}}_{a,t} + \left(\sum_{i=1}^{2} \frac{\partial \mathbf{J}(\mathbf{q}_{a,t})}{\partial q_{a,t}^{(i)}}\dot{q}_{a,t}^{(i)}\right)\dot{\mathbf{q}}_{a,t},$$

is the acceleration of the end-effector, where  $\mathbf{J}(\mathbf{q}_{a,t})$  is the Jacobian of the forward kinematic model.

The following three estimates are compared to the true position

 $\mathcal{T}_{\text{TCP}}(\hat{\mathbf{q}}_{\text{EKF},t}), \quad \mathcal{T}_{\text{TCP}}(\hat{\mathbf{q}}_{\text{PF},t}), \text{ and } \mathcal{T}_{\text{TCP}}(\mathbf{q}_{m,t}),$ 

where  $\mathcal{T}_{TCP}(\cdot)$  is the forward kinematic model. The true position is measured with a laser tracking system from Leica Geosytems.

Results

#### **AREA 6: Complex Engineering Systems**

$$\left( \mathbf{b}_{\ddot{
ho},t}^{T}
ight) ^{T},$$

$$\mathbf{G}_{w,t}\mathbf{w}_t$$

$$\left( t,t\right) ,$$

- better.
- The PF is closer to the true path.
- whereas the PF is much slower.



# **Future Work**

#### **Estimation**

- of 1) observability and 2) optimal sensor positioning.
- trol.

#### Control

- turbances.

The practical work will be together with Lund University and ABB Robotics.



• The EKF and PF track the entire path, i.e., the filters do not diverge. • The EKF has some problems in the corners, where the PF is much

• Implementing the EKF in MATLAB gives almost a real-time solution,

**6 DOF**: Estimation of a fully actuated serial manipulator.

Additional Sensors: Investigate the use of additional sensors in terms

**Real time:** Implementation aspects to get real time estimates for con-

**ILC:** Iterative Learning Control for control of repetitive errors and dis-

**Stiffness control:** Compliance control using estimated states.

**Disturbance rejection:** Attenuate the effect of disturbances.

**Path tracking:** Control the end-effector along a user defined path.

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